


```
MM      MM      TTTTTTTTTT  HH      HH      DDDDDDDDD  MM      MM      0000000  DDDDDDDDD
MM      MM      TTTTTTTTTT  HH      HH      DDDDDDDDD  MM      MM      0000000  DDDDDDDDD
MMMM    MMMM      TT          HH      HH      DD          DD  MMMM    MMMM  00          00  DD          DD
MMMM    MMMM      TT          HH      HH      DD          DD  MMMM    MMMM  00          00  DD          DD
MM      MM      TT          HH      HH      DD          DD  MM      MM      00          00  DD          DD
MM      MM      TT          HH      HH      DD          DD  MM      MM      00          00  DD          DD
MM      MM      TT          HHHHHHHHHHHH DD          DD  MM      MM      00          00  DD          DD
MM      MM      TT          HHHHHHHHHHHH DD          DD  MM      MM      00          00  DD          DD
MM      MM      TT          HH      HH      DD          DD  MM      MM      00          00  DD          DD
MM      MM      TT          HH      HH      DD          DD  MM      MM      00          00  DD          DD
MM      MM      TT          HH      HH      DD          DD  MM      MM      00          00  DD          DD
MM      MM      TT          HH      HH      DD          DD  MM      MM      00          00  DD          DD
MM      MM      TT          HH      HH      DDDDDDDDD  MM      MM      0000000  DDDDDDDDD
MM      MM      TT          HH      HH      DDDDDDDDD  MM      MM      0000000  DDDDDDDDD
                                     ....
                                     ....
                                     ....
                                     ....
```

```
LL      IIIIIII  SSSSSSSSS
LL      IIIIIII  SSSSSSSSS
LL      II       SS
LL      II       SS
LL      II       SS
LL      II       SS
LL      II       SSSSSSS
LL      II       SSSSSSS
LL      II       SS
LL      II       SS
LL      II       SS
LL      II       SS
LLLLLLLLLL  IIIIIII  SSSSSSSSS
LLLLLLLLLL  IIIIIII  SSSSSSSSS
```

(1)	49	HISTORY	; Detailed Current Edit History
(2)	54	DECLARATIONS	
(3)	89	MTM\$DMOD - D REAL*8 remainder	

```
0000 1      .TITLE MTH$DMOD
0000 2      .IDENT /3-001/
0000 3
0000 4      ; File: MTHDMOD.MAR Edit: JCW3001
0000 5      ;*****
0000 6      ;
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0000 23     ; SOFTWARE ON EQUIPMENT WHICH IS NOT SUPPLIED BY DIGITAL.
0000 24     ;
0000 25     ;*****
0000 26     ;
0000 27     ;
0000 28     ;
0000 29     ;++
0000 30     ; FACILITY: MATH LIBRARY
0000 31     ;
0000 32     ; ABSTRACT:
0000 33     ;
0000 34     ; This module contains the routine MTH$DMOD:
0000 35     ; It returns the remainder of the division of arg1/arg2 using
0000 36     ; the following equation:
0000 37     ;     arg1 - (int(arg1/arg2))*arg2
0000 38     ;
0000 39     ;
0000 40     ;--
0000 41     ;
0000 42     ; AUTHOR: Jeffrey C. Wiener, CREATION DATE: 21-DEC-1982
0000 43     ;
0000 44     ; MODIFIED BY:
0000 45     ;
0000 46     ;
0000 47     ;--
0000 48     ;
0000 49     ; .SBTTL HISTORY
0000 50     ;
0000 51     ; 3-001 Original version of complete re-write
0000 52     ;
```

; Detailed Current Edit History

JCW 21-DEC-82

DECLARATIONS

```
0000 54 .SBTTL DECLARATIONS
0000 55 :
0000 56 : INCLUDE FILES:
0000 57 :
0000 58 : NONE
0000 59 :
0000 60 : EXTERNAL SYMBOLS:
0000 61 :
0000 62 : .DSABL GBL ; Force all external symbols to be declared
0000 63 : .EXTRN MTH$$SIGNAL
0000 64 : .EXTRN MTH$K_FLOUNDMAT
0000 65 : .EXTRN MTH$K_INVARGMAT
0000 66 :
0000 67 : LIBRARY MACROS CALLS:
0000 68 :
0000 69 : $SFDEF ; Define SF$ (stack frame) symbols
0000 70 :
0000 71 : EQUATED SYMBOLS:
0000 72 :
00001B80 0000 73 : EXP 55 = ^X00001B80 ; 55*2^7
FFFF0FFF 0000 74 : HIGH_MASK = ^XFFFF0FFF
0000 75 :
0000 76 : OWN STORAGE:
0000 77 :
0000 78 : NONE
0000 79 :
0000 80 : PSECT DECLARATIONS:
0000 81 :
00000000 0000 82 : .PSECT _MTH$CODE PIC, SHR, LONG, EXE, NOWRT
0000 83 :
0000 84 : CONSTANTS:
0000 85 :
0000 86 TWO_EXP_55:
00000000 00005C00 0000 87 : .LONG ^X00005C00, ^X0 ; 2**55
```

MTH\$DMOD - D REAL*8 remainder

```
0008 89 .SBTTL MTH$DMOD - D REAL*8 remainder
0008 90 :++
0008 91 : FUNCTIONAL DESCRIPTION:
0008 92 :
0008 93 : Return the remainder of arg1/arg2 in D floating point format
0008 94 : Remainder = arg1 - (int(arg1/arg2))*arg2
0008 95 :
0008 96 : The algorithm used to evaluate the DMOD function is as follows:
0008 97 :
0008 98 : X = the first argument.
0008 99 : Y = the second argument.
0008 100 : step 1. m = the exponent of Y.
0008 101 : n = the exponent of X.
0008 102 : c = n - m
0008 103 : If c < 0, end with result = X.
0008 104 : step 2. I = the fractional part of X.
0008 105 : J = the fractional part of Y.
0008 106 : If I >= J, I = I - J
0008 107 : Go to step 5.
0008 108 : step 3. L = 2^(p-1)*I, where p = 56 for D_floating numbers.
0008 109 : step 4. T = L/J
0008 110 : T = [T+2^(p-1)]-2^(p-1). T is int(L/J) or int(L/J)+1
0008 111 : I = L - J * T
0008 112 : If I < 0, I = I + J T was int(L/J)+1
0008 113 : step 5. c = c - (p-1)
0008 114 : If c > 0 go to step 3.
0008 115 : step 6. If c = -(p-1) go to step 9.
0008 116 : step 7. L = 2^(p-1+c) * I
0008 117 : step 8. I = L - J * T
0008 118 : step 9. Result = 2^m * I
0008 119 :
0008 120 : CALLING SEQUENCE:
0008 121 :
0008 122 : Remainder.wd.v = MTH$DMOD (dividend.rd.r, divisor.rd.r)
0008 123 :
0008 124 : INPUT PARAMETERS:
0008 125 :
0008 126 : The two input parameters are double precision floating-point
0008 127 : values. They are passed by reference.
0008 128 :
0008 129 :
00000004 0008 130 : DIVIDEND = 4 ; Dividend = X in the algorithm.
00000008 0008 131 : DIVISOR = 8 ; Divisor = Y in the algorithm.
0008 132 :
0008 133 :
0008 134 : IMPLICIT INPUTS:
0008 135 :
0008 136 : NONE
0008 137 :
0008 138 : FUNCTION VALUE:
0008 139 :
0008 140 : Remainder of the division of arg1/arg2 is returned as a
0008 141 : double precision floating point value.
0008 142 :
0008 143 : IMPLICIT OUTPUTS:
0008 144 :
0008 145 :
```

MTH\$DMOD - D REAL*8 remainder

```
0008 146 : NONE
0008 147 :
0008 148 : COMPLETION CODES:
0008 149 :
0008 150 : NONE
0008 151 :
0008 152 : SIDE EFFECTS:
0008 153 :
0008 154 : MTH$_INVARGMAT - Invalid argument to math library if the divisor is zero.
0008 155 : MTH$_FLOUNDMAT - Floating underflow in math library is signaled if
0008 156 : the FU bit is set in the callers PSL.
0008 157 :
0008 158 :--
0008 159 :
01FC 0008 160 : .ENTRY MTH$DMOD, ^M<R2, R3, R4, R5, R6, R7, R8>
000A 161 :
52 08 BC 70 000A 162 : MOVD @DIVISOR(AP), R2 ; R2/R3 = Y
52 13 000E 163 : BEQL ERROR ; Y=0. Division by zero
50 04 BC 70 0010 164 : MOVD @DIVIDEND(AP), R0 ; R0/R1 = X
56 52 FFFF807F 8F CB 0014 165 :
58 50 FFFF807F 8F CB 001C 166 : BICL3 #^XFFF807F, R2, R6 ; R6=m is the biased exponent of Y
0024 167 : BICL3 #^XFFF807F, R0, R8 ; R8=n is the biased exponent of X
58 56 C2 0024 168 :
01 18 0027 169 : SUBL2 R6, R8 ; R4 = c = n-m unbiased
04 0029 170 : BGEQ STEP_2 ; Result is X if X<Y, ie, if c<0
002A 171 : RET ; R0/R1 = X
56 DD 002A 172 :
002C 173 : STEP_2: PUSHL R6 ; push m onto the stack
52 FF80 8F AA 002C 174 : BICW2 #^XFF80, R2 ; R2/R3 = J = unbiased !fract(Y)!
52 4000 8F AC 0031 175 : XORW #^X4000, R2 ; J = properly biased !fract(Y)!
50 FF80 8F AA 0036 176 :
50 4000 8F AC 003B 177 : BICW2 #^XFF80, R0 ; R0/R1 = I = unbiased !fract(X)!
0040 178 : XORW #^X4000, R0 ; I = properly biased !fract(X)!
0040 179 :
0040 180 :
0040 181 : :+
0040 182 :
0040 183 : In STEP_4 and STEP_8 the calculation of I = L - J*int(L/J) must be
0040 184 : computed as precisely as possible. To do this we will need to write J as
0040 185 : J = J1 + J2
0040 186 : where J1 = the high 24 bits of J and J2 = J - J1, the low 24 bits of J.
0040 187 :
0040 188 : HIGH_MASK is used to extract the 8 bits of J from longword2 that belong
0040 189 : to JT.
0040 190 :
0040 191 : :-
04 AE 7E 52 7D 0040 192 : MOVQ R2, -(SP) ; (SP) = J
7E 52 6E 63 0043 193 : BICL #HIGH_MASK, 4(SP) ; (SP) = J1 replaces the value
004B 194 : ; of J on the top of the SP
7E 52 6E 63 004B 195 : SUBD3 (SP), R2, -(SP) ; (SP) = J2 = J - J1
52 50 71 004F 196 :
52 63 19 004F 197 : CMPD R0, R2 ; If I<J
50 52 62 0052 198 : BLSS STEP_5 ; go to STEP_5
5E 14 0054 199 : SUBD2 R2, R0 ; else I = I-J
0057 200 : BGTR STEP_5 ; go to STEP_5 if I>0, or
0059 201 : ; else the algorithm ends
04 BC B5 0059 202 : TSTW @DIVIDEND(AP) ; the sign of the result is
```


MTHSDMOD - D REAL*8 remainder

```

      50 03 18 005C 203 BGEQ DONE ; the same as the sign of
      50 50 72 005E 204 MNEGD RO, RO ; the first argument, A.
      04 0061 205 DONE: RET
      0062 206
      50 01 0F 79 0062 207 ERROR: ASHQ #15, #1, R0 ; Y=0. Reserved operand
      7E 00 8F 9A 0066 208 MOVZBL #MTH$K INVARGMAT, -(SP) ; error code
00000000 GF 01 FB 006A 209 CALLS #1, G^MTH$$SIGNAL ; signal the error
      04 0071 210 RET
      0072 211
      50 00001B80 8F C0 0072 212 STEP_3: ADDL2 #EXP_55, R0 ; R0/R1 = L = 2**((p-1)*I
      0079 213
      0079 214 :+
      0079 215 :+
      0079 216 :+
      0079 217 :+
      0079 218 :+
      0079 219 :+
      0079 220 :-
      0079 221
      56 50 52 67 0079 222 DIVD3 R2, R0, R6 ; R6/R7 = T = L/J
      56 80 AF 60 007D 223 ADDD2 TWO_EXP_55, R6 ; R6/R7 = T = T+2**((p-1)
      56 FF7B CF 62 0081 224 SUBD2 TWO_EXP_55, R6 ; T-2**((p-1) = L/J chopped or choppe
      0086 225
      0086 226 :+
      0086 227 :+
      0086 228 :+
      0086 229 :+
      0086 230 :+
      0086 231 :+
      0086 232 :+
      0086 233 :+
      0086 234 :+
      0086 235 :+
      0086 236 :+
      0086 237 :+
      0086 238 :+
      0086 239 :+
      0086 240 :-
      0086 241
      55 57 54 56 D0 0086 242 MOVL R6, R4
      FFFF0FFF 8F CB 0089 243 BICL3 #HIGH_MASK, R7, R5 ; R4/R5 = Z1
      56 54 62 0091 244 SUBD2 R4, R6 ; R6/R7 = Z2
      7E 08 AE 54 65 0094 245 MULD3 R4, 8(SP), -(SP) ; Compute Z1*J1
      50 8E 62 0099 246 SUBD2 (SP)+, R0 ; R0/R1 = L - Z1*J1
      54 6E 64 009C 247 MULD2 (SP), R4 ; R4/R5 = Z1*J2
      50 54 62 009F 248 SUBD2 R4, R0 ; R0/R1 = L - Z1*J
      54 56 08 AE 65 00A2 249 MULD3 8(SP), R6, R4 ; R4/R5 = Z2*J1
      50 54 62 00A7 250 SUBD2 R4, R0 ; R0/R1 = L - Z1*J - Z2*J1
      56 6E 64 00AA 251 MULD2 (SP), R6 ; R6/R7 = Z2*J2
      50 56 62 00AD 252 SUBD2 R6, R0 ; R0/R1 = L - Z*J
      05 14 00B0 253 BGTR STEP_5
      50 6D 13 00B2 254 BEQL RETURN
      50 52 60 00B4 255 ADDD R2, R0 ; End if R0/R1=0
      00B7 256 ; Add J back in because you had
      00B7 257 ; T=chopped(L/J)+1
      58 00001B80 8F C2 00B7 258 STEP_5: SUBL2 #EXP_55, R8 ; c = c-(p-1) = c-55
      B2 18 00BE 259 BGEQ STEP_3
```


MTH\$DMOD - D REAL*8 remainder

```
58 00001B80 8F C0 00C0 260 ADDL2 #EXP_55, R8 ; c = (p-1)+c = 55+c
    00C7 261
    00C7 262 :+
    00C7 263 :+
    00C7 264 :+
    00C7 265 :+
    00C7 266 :-
    00C7 267
    50 42 13 00C7 268 BEQL STEP_9 ; L = I*2^(c+t)
    58 58 C0 00C9 269 ADDL2 R8, R0
    00CC 270
    00CC 271 :+
    00CC 272 :+
    00CC 273 :+
    00CC 274 :-
    00CC 275
    56 50 52 67 00CC 276 DIVD3 R2, R0, R6 ; R6/R7 = T = L/J
    56 FF2C CF 60 00D0 277 ADDD2 TWO_EXP_55, R6 ; R6/R7 = T = T+2**(p-1)
    56 FF27 CF 62 00D5 278 SUBD2 TWO_EXP_55, R6 ; T-2**(p-1) = L/J chopped or choppe
    00DA 279
    00DA 280 :+
    00DA 281 :+
    00DA 282 :+
    00DA 283 :+
    00DA 284 :+
    00DA 285 :+
    00DA 286 :+
    00DA 287 :+
    00DA 288 :+
    00DA 289 :+
    00DA 290 :+
    00DA 291 :+
    00DA 292 :+
    00DA 293 :+
    00DA 294 :+
    00DA 295 :+
    00DA 296 :-
    00DA 297
    55 57 FFFF0FFF 54 56 D0 00DA 298 MOVL R6, R4
    7E 08 AE 54 62 00DD 299 BICL3 #HIGH_MASK, R7, R5
    50 8E 65 00E5 300 SUBD2 R4, R6
    54 6E 62 00E8 301 MULD3 R4, 8(SP), -(SP)
    50 54 64 00ED 302 SUBD2 (SP)+, R0
    54 54 62 00F0 303 MULD2 (SP), R4
    50 54 62 00F3 304 SUBD2 R4, R0
    54 56 08 AE 65 00F6 305 MULD3 8(SP), R6, R4
    50 54 62 00FB 306 SUBD2 R4, R0
    56 6E 64 00FE 307 MULD2 (SP), R6
    50 56 62 0101 308 SUBD2 R6, R0
    05 14 0104 309 BGTR STEP_9
    19 13 0106 310 BEQL RETURN
    50 52 60 0108 311 ADDD R2, R0
    010B 312
    010B 313
    10 AE 4000 8F A2 010B 314 STEP_9: SUBW #*X4000, 16(SP)
    50 10 AE A0 0111 315 ADDW2 16(SP), R0
    0B 19 0115 316 BLSS UNDERFLOW
```

The next two lines of code are STEP_6 and STEP_7.

$2^{(p-1)} = 2^{(55)}$ is added and then subtracted from
 $T = \text{int}(L/J)$ to ensure that $T = \text{chopped}(L/J)$ or $\text{chopped}(L/J)+1$

STEP_8:

The calculation of $I = L - J * \text{int}(L/J)$ must be computed as precise as possible. To do this we will need to write T as
 $T = Z1 + Z2$
where $Z1$ = the high 24 bits of T and $Z2 = T - Z1$, the low 24 bits of T .

Now, using $J = J1 + J2$,

$$\begin{aligned} L - J * \text{int}(L/J) &= L - (J1 + J2) * (Z1 + Z2) \\ &= L - (Z1 * J1) - (Z1 * J2) \\ &\quad - (Z2 * J1) - (Z2 * J2) \\ &= L - (Z1 * J) - (Z2 * J) \end{aligned}$$

R4/R5 = Z1
R6/R7 = Z2
Compute Z1*J1
R0/R1 = L - Z1*J1
R4/R5 = Z1*J2
R0/R1 = L - Z1*J
R4/R5 = Z2*J1
R0/R1 = L - Z1*J - Z2*J1
R6/R7 = Z2*J2
R0/R1 = L - Z*J

End if R0/R1=0
Add J back in because you had
 $T = \text{chopped}(L/J)+1$

Remove bias from m and
form $R0/R1 = 2^m * L$
Branch if underflow

MTH\$DMOD - D REAL*8 remainder

```

      04 BC  B5 0117 317 TEST_SIGN:
      05 18 0117 318 TSTW @DIVIDEND(AP) ; the sign of the result is
50 8000 8F A8 011A 319 BGEQ RETURN ; the same as the sign of
      04 011C 320 BLSW2 #^X8000, R0 ; the first argument, X.
      0121 321 RETURN: RET
      0122 322
      0122 323 UNDERFLOW:
      0122 324 CLRQ R0 ; Set up default result to 0.0
OD 04 AD 50 7C 0122 325 BBC #SF$V_FU, SF$W_SAVE_PSW(FP), NO_FU ; Branch if caller has not enabled F
      06 E1 0124 326
      00000000'8F DD 0129 327 PUSHL #MTH$K_FLOUNDMAT ; Report MTH$_FLOUNDMAT
00000000'GF 01 FB 012F 328 CALLS #1, G^MTH$$SIGNAL ; Signal the condition
      04 0136 329 NO_FU: RET ; Return
      0137 330
      0137 331 .END
```

MTH\$DMOD
Symbol table

E 10

16-SEP-1984 01:19:04 VAX/VMS Macro V04-00
6-SEP-1984 11:22:24 [MTHRTL.SRC]MTHDMOD.MAR;1

Page 8
(3)

```

DIVIDEND      = 00000004
DIVISOR       = 00000008
DONE          = 00000061 R    02
ERROR         = 00000062 R    02
EXP_55        = 00001B80
HIGH_MASK     = FFFF0FFF
MTH$SIGNAL    = ***** X    00
MTH$DMOD      = 00000008 RG   02
MTH$K_FLOUNDMAT = ***** X    00
MTH$K_INVARGMAT = ***** X    00
NO_FU         = 00000136 R    02
RETURN        = 00000121 R    02
SF$V_FU       = 00000006
SF$W_SAVE_PSW = 00000004
STEP-2        = 0000002A R    02
STEP-3        = 00000072 R    02
STEP-5        = 000000B7 R    02
STEP-9        = 0000010B R    02
TEST_SIGN     = 00000117 R    02
TWO_EXP_55    = 00000000 R    02
UNDERFLOW     = 00000122 R    02

```

! Psect synopsis !

PSECT name	Allocation	PSECT No.	Attributes
. ABS .	00000000 (0.)	00 (0.)	NOPIC USR CON ABS LCL NOSHR NOEXE NORD NOWRT NOVEC BYTE
\$ABSS	00000000 (0.)	01 (1.)	NOPIC USR CON ABS LCL NOSHR EXE RD WRT NOVEC BYTE
_MTH\$CODE	00000137 (311.)	02 (2.)	PIC USR CON REL LCL SHR EXE RD NOWRT NOVEC LONG

! Performance indicators !

Phase	Page faults	CPU Time	Elapsed Time
Initialization	34	00:00:00.09	00:00:01.54
Command processing	117	00:00:00.45	00:00:03.28
Pass 1	122	00:00:01.45	00:00:05.82
Symbol table sort	0	00:00:00.03	00:00:00.19
Pass 2	72	00:00:00.71	00:00:03.37
Symbol table output	3	00:00:00.03	00:00:00.07
Psect synopsis output	3	00:00:00.02	00:00:00.02
Cross-reference output	0	00:00:00.00	00:00:00.00
Assembler run totals	353	00:00:02.79	00:00:14.30

The working set limit was 900 pages.
6542 bytes (13 pages) of virtual memory were used to buffer the intermediate code.
There were 10 pages of symbol table space allocated to hold 48 non-local and 0 local symbols.
331 source lines were read in Pass 1, producing 13 object records in Pass 2.
8 pages of virtual memory were used to define 7 macros.

! Macro library statistics !

Macro library name

Macros defined

_\$255\$DUA28:[SYSLIB]STARLET.MLB;2

4

88 GETS were required to define 4 macros.

There were no errors, warnings or information messages.

MACRO/ENABLE=SUPPRESSION/DISABLE=(GLOBAL,TRACEBACK)/LIS=LIS\$:MTHDMOD/OBJ=OBJ\$:MTHDMOD MSRC\$:MTHDMOD/UPDATE=(ENH\$:MTHDMOD)

AH-BT13A-SE
VAX/VMS V4.0

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